

The *curve graph*  $C(S)$  of a closed orientable surface  $S$  is the graph whose vertices correspond to closed curves in  $S$  satisfying certain simple conditions. Edges join vertices that have disjoint representatives on  $S$ . Each edge is defined to have length 1. The distance  $d(v, w)$  is defined to be the number of edges in a shortest path in the curve graph from  $v$  to  $w$ . Any such path is called a *geodesic*. The intersection number of  $v$  and  $w$ , denoted  $i(v, w)$ , is simply the number of intersections of the two curves as they travel along the surface.

We highlight a new relationship between the distance  $d(v, w)$  of a filling pair of curves  $v$  and  $w$  in  $C(S)$  and the surface decomposition of  $S$  into polygons that is induced by cutting  $S$  open along  $v$  and  $w$ . The main result is the discovery and analysis of particular configurations of rectangles in the decomposition, called *spirals*. We show that adding spirals, an operation which always increases intersection number, can increase distance or can send intersection number to infinity, leaving distance unchanged. This talk is based on *Distance and intersection number in the curve graph of a surface*, joint with Joan Birman (Columbia University) and Matt Morse (New York University).